

Grammar in a Landscape of Affordances

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<https://elenigregor.github.io/>

<http://dynamicsyntax.org/>

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- 1 DS-TTR
- 2 Zoom into trees and treenodes
- 3 DS-TTR+
- 4 Appendix

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what is the nature of grammar: the view from DS-TTR

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- grammatical/metaphysical ontology of **processes**
 - rather than *representations*

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- grammatical/metaphysical ontology of **processes**
 - rather than *representations*
- **incrementality, underspecification, and predictivity** as properties of the grammar
- domain-general processes for **multimodal interaction**
[e.g., Yu et al. (2015, 2017); Yu et al., 2016]]
- learnable from minimal data via Reinforcement Learning
[e.g., Kalatzis et al. (2016); Eshghi et al. (2017b)]

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- no separate **syntactic level of representation**:
 - no syntactic categories for strings of words;
 - no phrase-structure rules;
 - sequences of words are not sequences of symbols but sequences of **affordance triggers**

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- **grammatical affordances** are dynamic regularities extending over multiple time-steps

extending DS-TTR: conceptualisation as interaction

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 - affordances are the possibilities for interaction in the sociomaterial environment to which agents are “attuned”
 - interaction with entities
 - agents can interact with aspects of entities without necessarily recognising the entity
 - learning affordances (sensorimotor contingencies) replaces the effort of building ontologies and writing rules
- types (concepts) as **time-extended processes** (incrementality, temporality)

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- at each time-step, affordances need to be **selected** from a landscape of possible affordances

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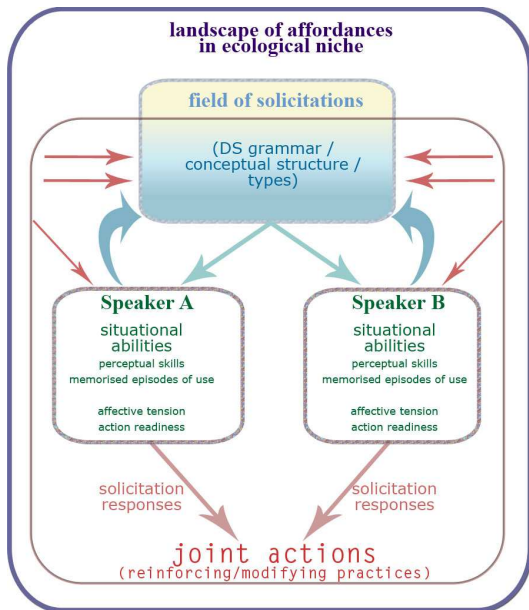
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- so-called *common ground* Stalnaker (1999); Clark (1996)] is a property of the relation of individual participants' affordances
- incrementality and temporality means that such fields are **redefined** and **transformed** with each utterance (verbal or otherwise)



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- **interactions**: both comprehension and production modelled together in the same space
- syntactic or meaning procedures formulated as (probabilistic) **transitions** from states to states

- a specialised **Propositional Dynamic Logic (PDL)** with states as $\langle \text{NL string, context} \rangle$ and transition operators modelling basic actions and macros (packages) of such actions

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- Dynamic Logics

- have the means to model any type of action and event (physical, instrumental, epistemic, etc.) [e.g. Segerberg (1992)]: hence multimodal grammar definitions are seamless
- model an internal perspective in a computation, an observer's view located at a state (node) considering the possibilities
- potential to bring Dynamic Quantum Logic [Baltag and Smets (2012)] to interface with DS Vector Space Semantics

[Purver et al. (forthcoming); Sadrzadeh et al. (2018); Gregoromichelaki et al. (2019a)]

- however, ideally, the π -calculus might be more suitable

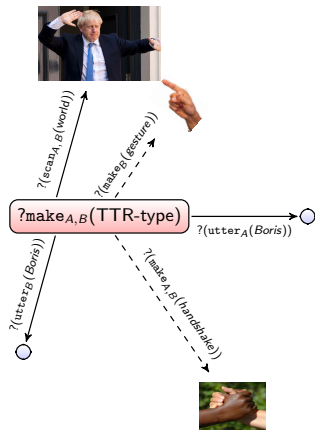
fractal structure of state transition system

(red path indicates the selected course of action)

?make_{A,B}(TTR-type)

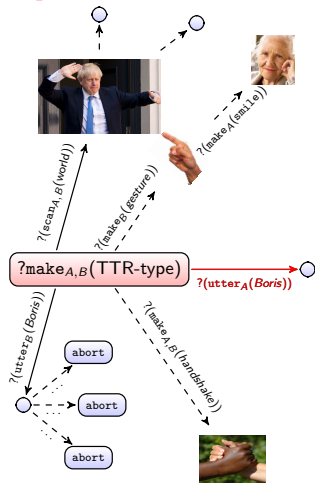
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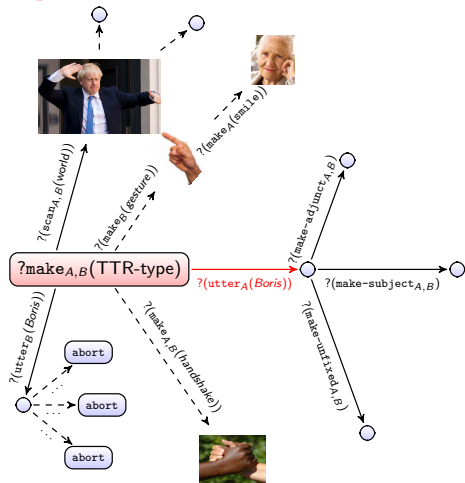
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Alice to Bob: "Boris!"

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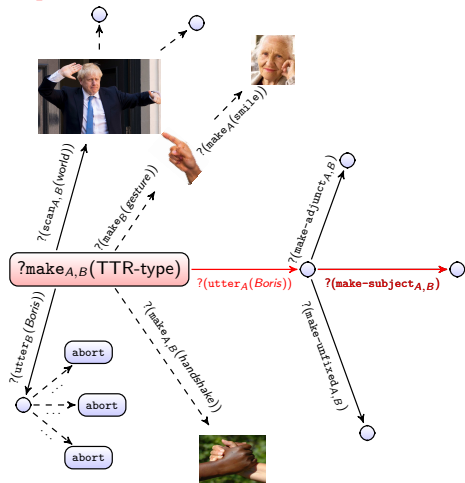
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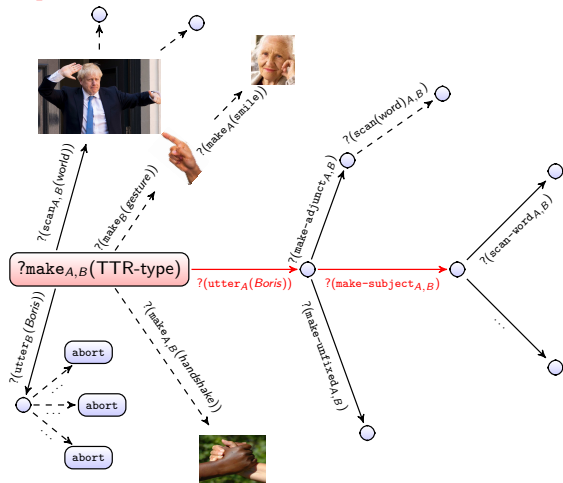
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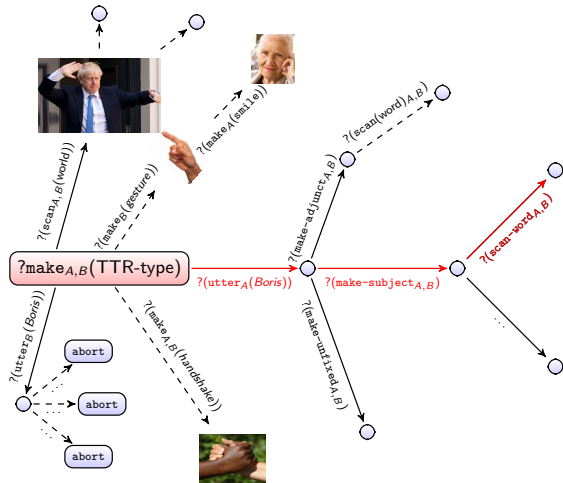


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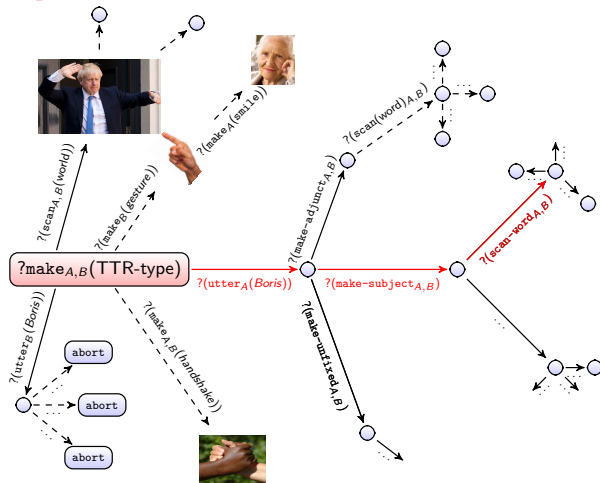
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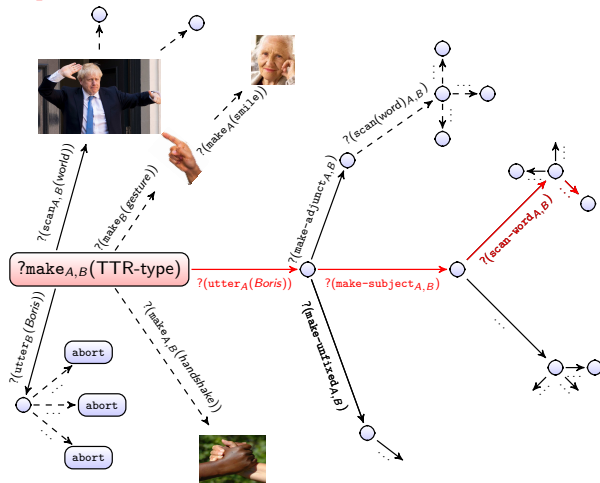
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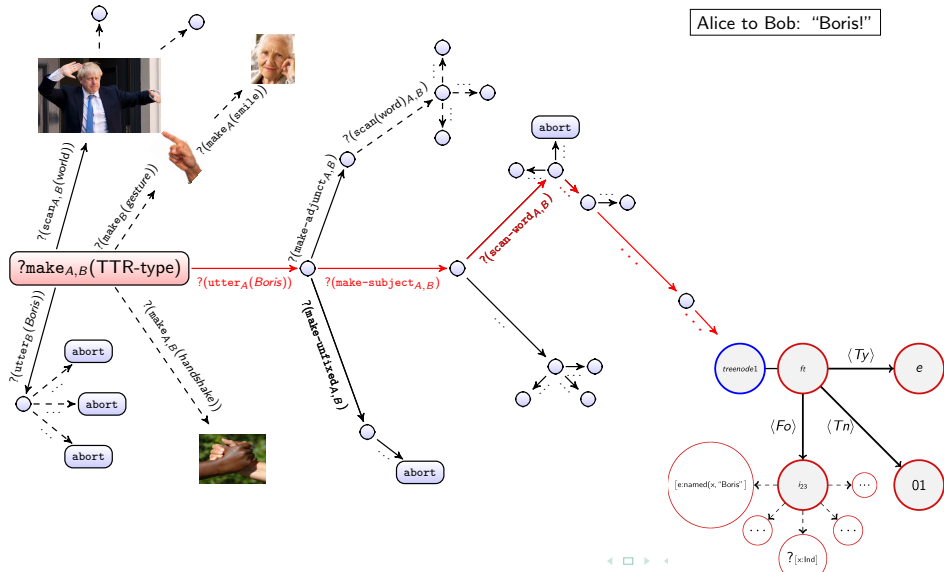
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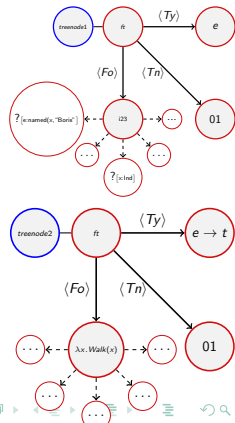
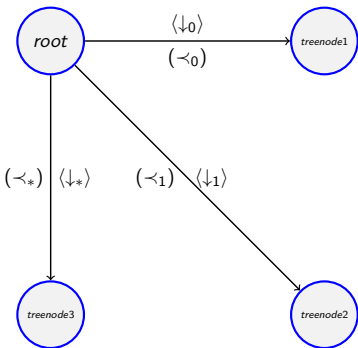
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actions first

- DS explains all allegedly syntactic phenomena as properties of processing mechanisms or the structuration of affordances into hierarchical structures
- (partial) **tree-structures** emerge as an intermediate structural bottleneck in the DS-TTR landscape of affordances
 - trees express the bifurcation of processes



actions first

- actions as first-class citizens

actions first

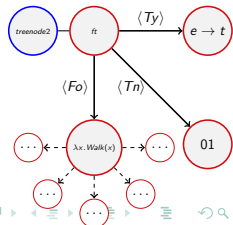
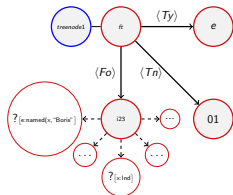
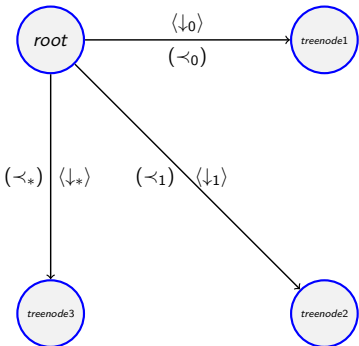
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 - actions can refer to actions (for, e.g. sloppy ellipsis)
 - the grammar can talk about the grammar (for, e.g., “metalinguistic” quotation)
- (if necessary,) representation as an aspect of successful interaction [Bickhard (2009)] via predictivity



DS-TTR: parsing and generation

- from **strings** to **conceptual structure** (TTR) or vice-versa

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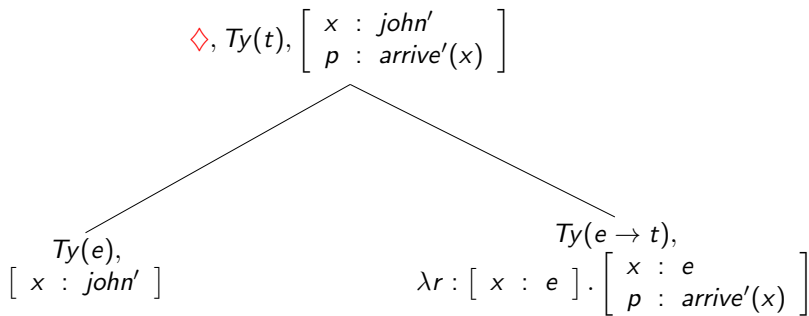
John arrived.

DS-TTR: parsing and generation

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John arrived.

John arrived
 \mapsto



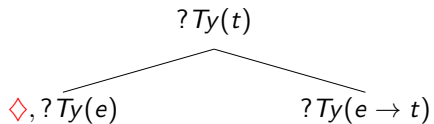
incremental construction

[START] ... PREDICTION
 \longmapsto

$\diamond, ?Ty(t)$

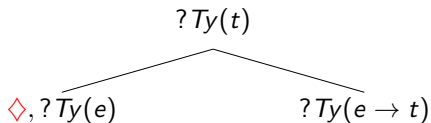
incremental construction

PREDICTION
 $\vdash \rightarrow$



incremental construction

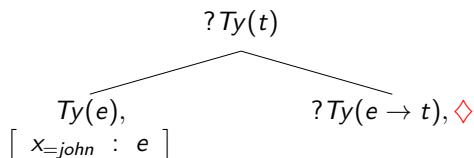
John
→



```
John IF      ?Ty(e)
      THEN  put(Ty(e))
           put([ x=john : e ])
      ELSE  abort
```

incremental construction

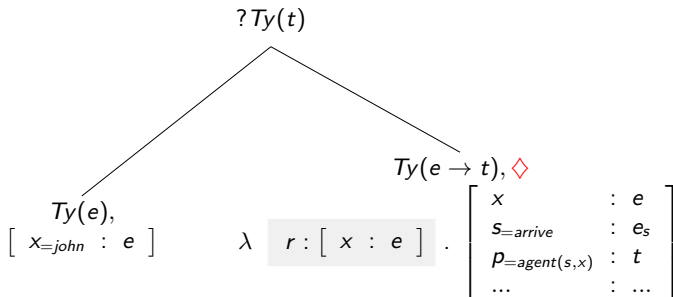
John, ..., POINTER-MOVEMENT
┆→



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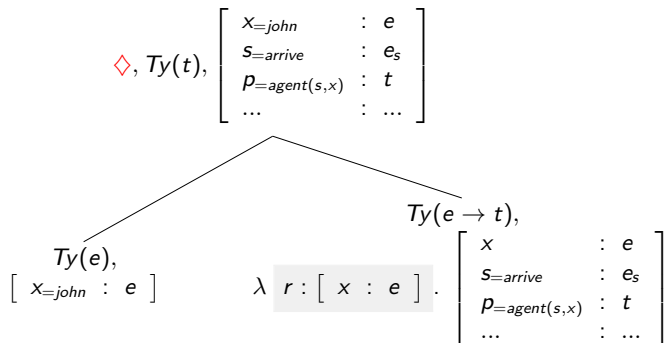
incremental construction

..., ..., arrives
→



incremental construction

...[TENSE, ...], COMPLETION
→



underspecification: structural

- processing **non-contiguous dependencies**
 - e.g. 'Mary, John upset'

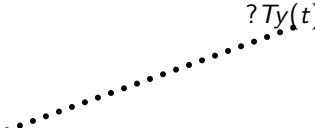
? $Ty(t)$, \diamond

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$[x : \text{mary}']$, \diamond

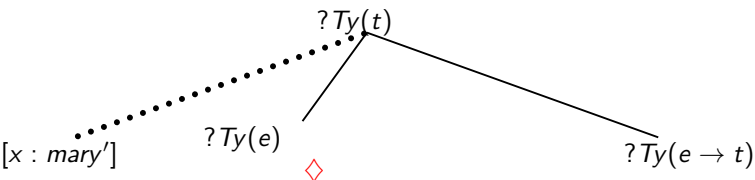


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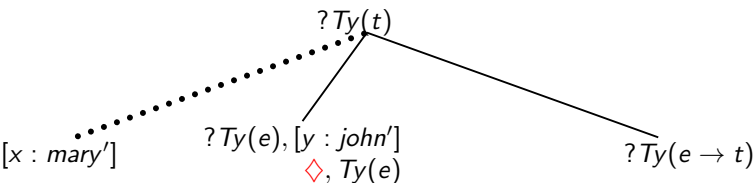


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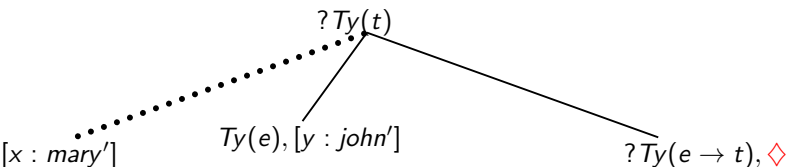


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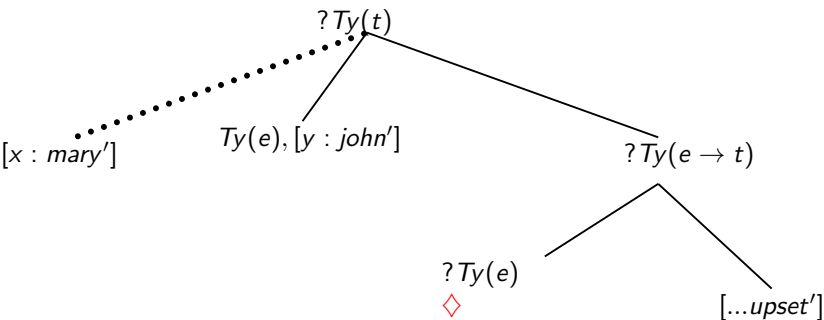


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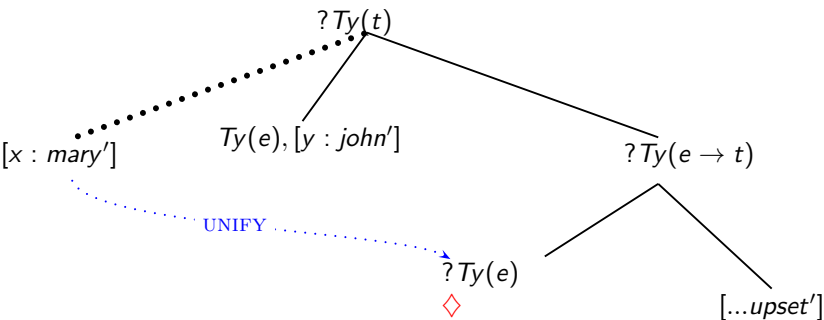


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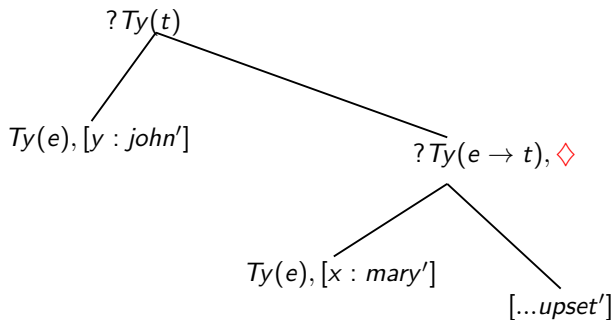


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$Tn(0), Ty(t), [upset'(mary')(john')], \diamond$

$Ty(e), [y : john']$

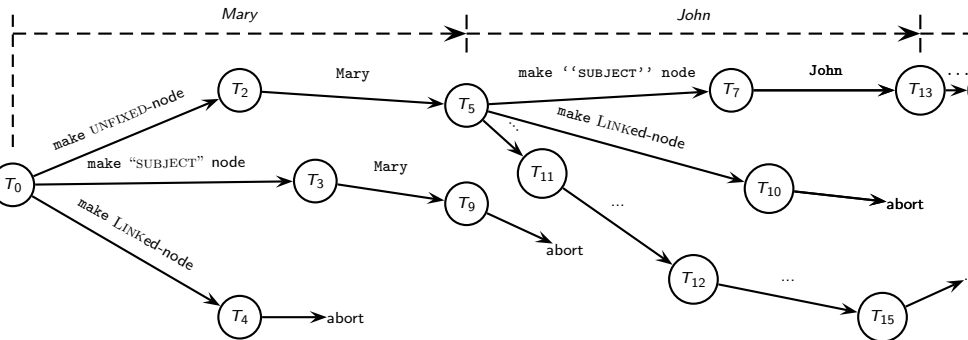
$Ty(e \rightarrow t), [...upset'(mary')]$

$Ty(e), [x : mary']$

$[...upset']$

a field of affordances

(simplified) options for starting to parse/produce *Mary, John upset*



utterance micro-events

$$\diamond, Ty(t), \left[\begin{array}{l} \text{CONTEXT : } u_1 \oplus u_2 \\ \text{CONTENT : } \left[\begin{array}{l} x : e \\ p : f(x) \end{array} \right] \end{array} \right]$$

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$$Ty(e \rightarrow t), \left[\begin{array}{l} \text{CONTEXT : } u_1 \\ \text{CONTENT : } \lambda r : [x : e] . \left[\begin{array}{l} x : e \\ p : f(x) \end{array} \right] \end{array} \right]$$

including contextual parameters

John arrived



◇, $Ty(t)$,

CONTEXT :

a : participantA

b : participantB

... : ...

u_1 : *utt* – event

s_{s1} : *spkr*(u_1 , a)

s_{a1} : *addr*(u_1 , b)

u_2 : *utt* – event

s_{s2} : *spkr*(u_2 , a)

s_{a2} : *addr*(u_2 , b)

... : ...

CONTENT :

x : john

p : *arrive*(x)

$Ty(e)$,

CONTEXT :

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s_{s1} : *spkr*(u_1 , a)

... : ...

CONTENT : x : john

$Ty(e \rightarrow t)$,

CONTEXT :

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... : ...

s_{s2} : *spkr*(u_2 , a)

... : ...

CONTENT : $\lambda r : [x : e]. [p : arrive(x)]$

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 - they are agent-relative (perspectival) properties of the environment [(Chemero, 2010)]
- types are not paired instantaneously with labels: types induce fields of potential paths of interaction with patterns in the environment
 - “the whole system of input and output resonates to the external information” [Gibson, 1966: 5].

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- states are partially ordered
- states are structured objects
 - e.g., in DS, states are decorated partial trees which map to more elaborate trees as you go along

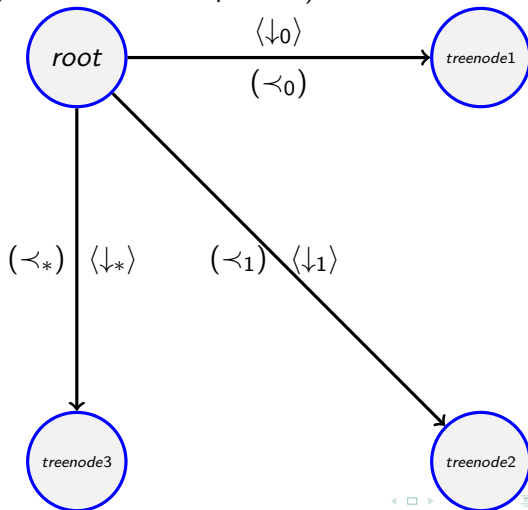
logical structure of DS: trees

NL: actions from an initial state to a result state

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- in DS, states are partial trees (in the description language DU, they are accessed by means of modal operators)



logical structure of DS: treenodes

- DS **trees** are sets of states related by dominance (modal) operators
- in turn, each **tree node** is inhabited by a feature structure
 - an instance of “fibred semantics” [Finger, Marcelo and Gabbay, Dov (1992)]
- **feature structures** are labelled directed graphs
- features (partial functions) like Fo , Tn , Ty , ...
 - nesting of features is possible
- values (“decorations”) like e , $eleni'$, 010, ...
- AVM notation:

$$tn_{01}: \left[\begin{array}{ll} Type & e \rightarrow t \\ Formula & \lambda x Walk(x) \\ TreeNode & 01 \end{array} \right]$$

logical structure of DS: decorations

- a treenode is a state

logical structure of DS: decorations

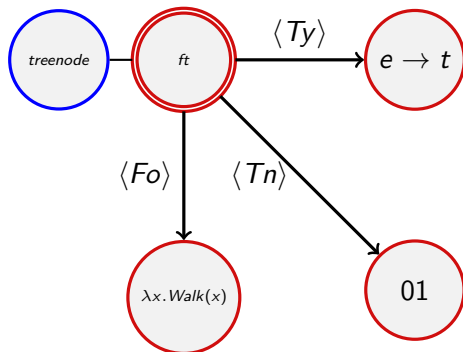
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- besides resolved feature structures, each treenode is also assigned a set of **requirements**
- all (atomic) decorations can appear as requirements

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- AVM notation:

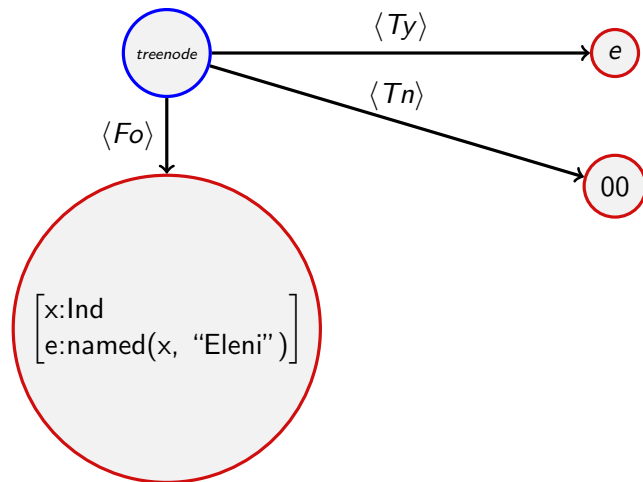
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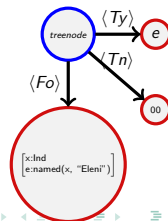
- $DU_F(?)$ language notation
 $\langle Tn \rangle(01) \bullet ?\langle Ty \rangle(e), ?\exists(\mathbf{x})\langle Fo \rangle(\mathbf{x})$

DS-TTR: TTR types as Fo values



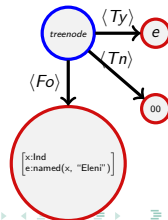
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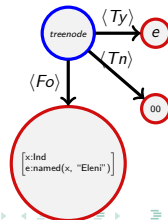
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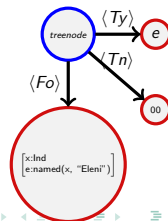
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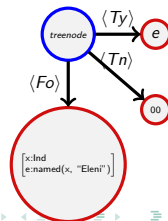
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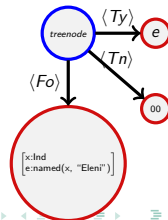
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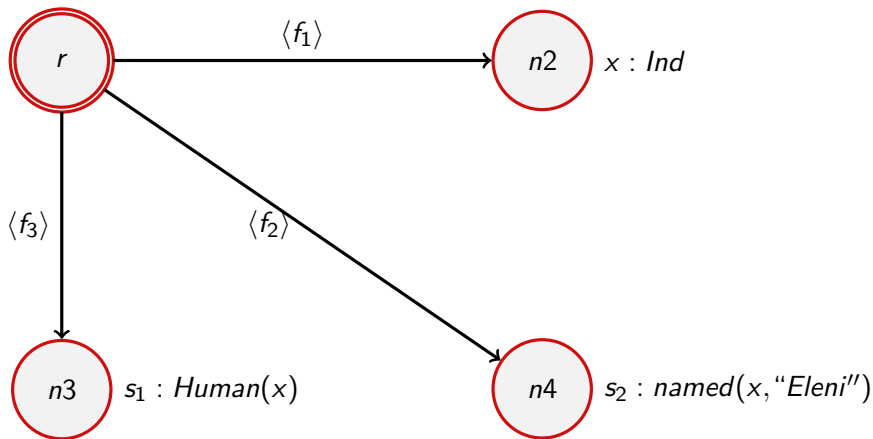
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- moving along the subtype relation
 - introduce requirements to impose further specification
- additionally, we can “internalise” trees in TTR types so that it is whole TTR types that are extended by DS actions



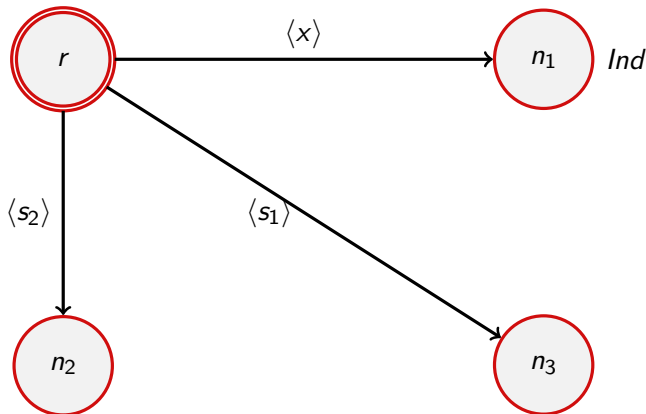
logical structure of TTR: version 1 (conservative)

- assign syntactic structure to **record types**
- **typing judgements** are propositions that hold at nodes
- fields are indexed



logical structure of TTR: version 2a

- a **record type** is a state (an initial, base, state)
- labels (discourse referents) are represented as modal operators (features)
- entities are nodes

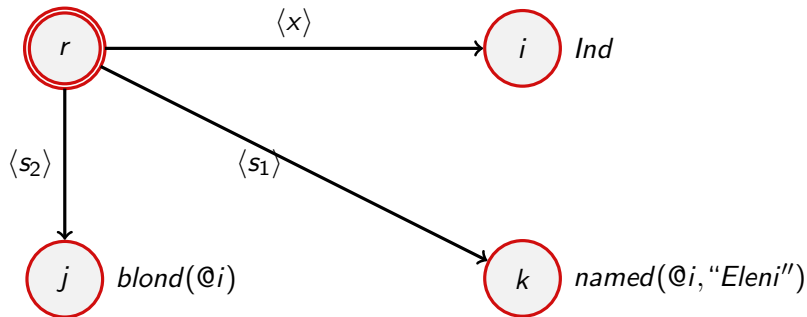


$$\lambda z. \text{blond}(z) \wedge \langle z : \langle s_2 \rangle \langle x \rangle : \triangleq \langle 0 \rangle n_1 \rangle$$

$$\lambda y. \text{named}(y, \text{"Eleni"}) \wedge \langle y : \langle s_1 \rangle \langle x \rangle : \triangleq \langle 0 \rangle n_1 \rangle$$

logical structure of TTR: version 2b

- a **record type** is a state (an initial state)
- labels are represented as modal operators
- node names are *nominals* in Hybrid Logic [(Blackburn, 2000)]
 - this will bring us close to the Duesseldorf Frames implementation [Kallmeyer and Osswald (2013); Kallmeyer et al. (2015)]
- types are (predicates of) states:



- but then do we still need labels?

- ontology

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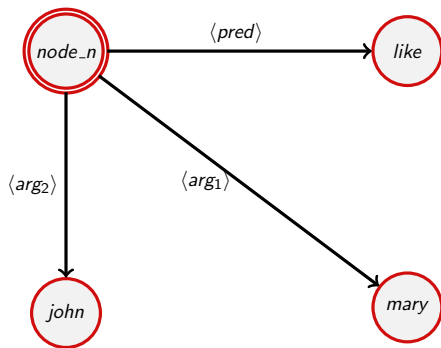
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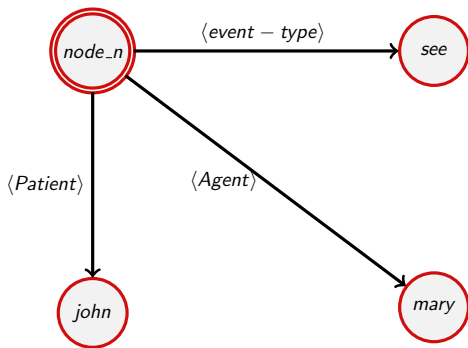
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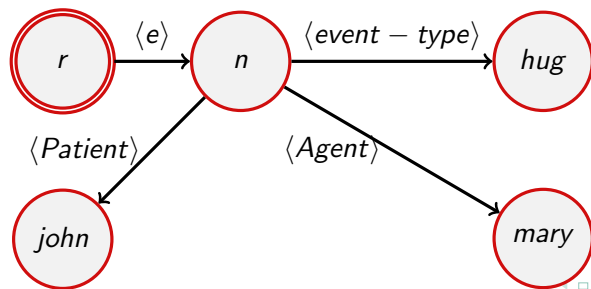
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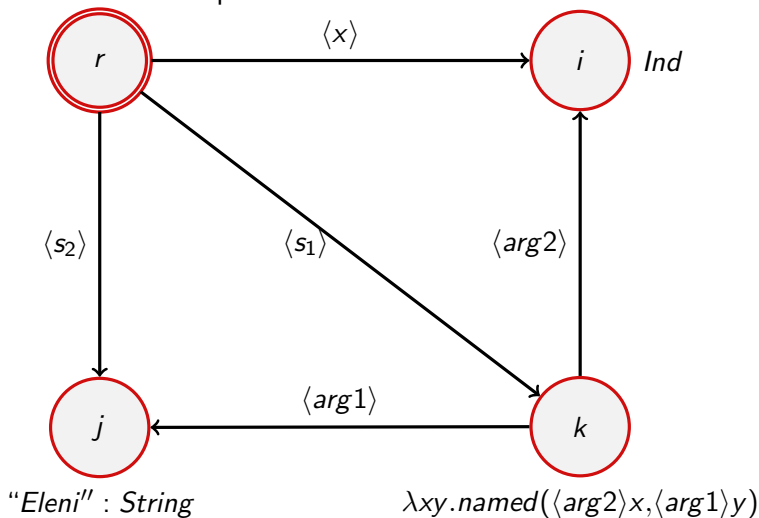
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logical structure of TTR: version (4a)

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logical structure of TTR: situational version 4b

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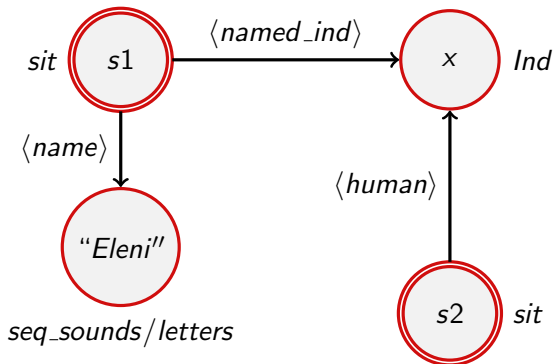
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- for each program α and each formula (tree, TTR-type) φ , $\langle \alpha \rangle \varphi$ or $\langle do(\alpha) \rangle \varphi$ is a formula
 - this means that there is an execution of program α that ends in a state where φ holds

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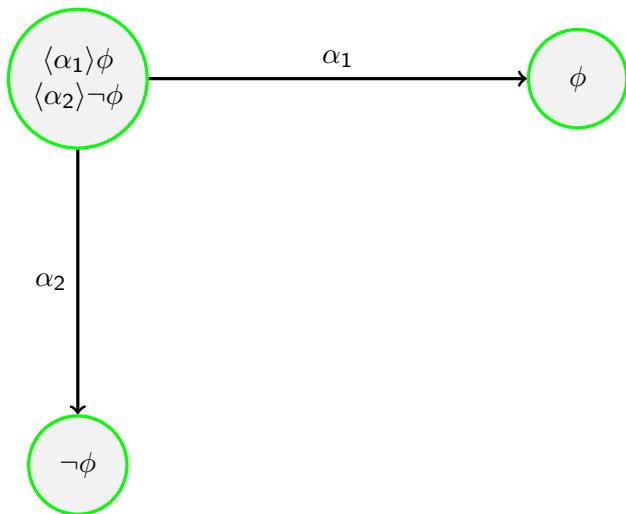
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actions as modal operators in DS



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- remove restriction that elimination of requirements (predictions) is criterion of wellformedness
 - requirements are constantly generated and always present to guide further development

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- e.g., for coverbal gestures, exploit ASL formalisation of gesture formats and assign interpretations, e.g., social relation affordances instituted

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- form the language $L^{DS-TTR}(L_{DS}(TTR), AG, ACT)$, based on the sets of propositions ($L_{DS}(TTR)$), agents (AG), and atomic DS actions (ACT)
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- the language contains:
 - (at least) the propositional connectives (plus TTR operations), the execution and result operator $\langle do_(-) \rangle$, the ability operator $AB_$, the action constructors:
 - $confirm_$ (confirmations/tests),
 - $;-$ (sequential composition),
 - $if_ then_ else_$ (conditional composition) and
 - $while_ do_$ (repetitive composition)

the language $L^{\text{DS-TTR}}$

- introduce all the propositional connectives:
- $\varphi, \psi \in L^{\text{DS-TTR}}$ implies
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(1a) DS

```
IF      ?Ty(e)  
THEN   put(Ty(e))  
        put(Fo(john'))  
ELSE   abort
```


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(1b) DS-TTR

```
IF      ?Ty(e)
THEN    put(Ty(e))
        put(Fo([ x : john ]))
ELSE    abort
```

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$$\left[\begin{array}{l} \text{sp-event} = e \\ \text{cont} = \left[\begin{array}{l} \text{bg} = \left[\begin{array}{l} x : \text{Ind} \\ \text{e} : \text{named}(x, \text{"Eleni"}) \end{array} \right] \\ \text{fg} = \lambda r : \left[\begin{array}{l} x : \text{Ind} \\ \text{e} : \text{named}(x, \text{"Eleni"}) \end{array} \right] . r.x \end{array} \right] \end{array} \right] : \left[\begin{array}{l} \text{"Eleni"} \\ \text{bg} : \text{RecType} \\ \text{fg} : (\text{bg} \rightarrow \text{Ind}) \end{array} \right]$$

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$\langle f_1, \langle label : Type \rangle \rangle$

- record types are sets of fields
- lexical entry for proper name:

```
IF      ?Ty(e)  $\wedge$   $\langle do_H(\text{hear}) \rangle$  "Eleni"  
THEN   ? $\langle do_{S\&H}(\text{make-go}) \rangle$ ( $\langle f_1 \rangle$ ); put(?ABS&H([x:Ind])),  
       ? $\langle do_{S\&H}(\text{make-go}) \rangle$ ( $\langle f_2 \rangle$ ); put?ABS&H([s1:(named(x, "Eleni"))])  
       ? $\langle do_{S\&H}(\text{make-go}) \rangle$ ; put?ABS&H([s2:(acquainted(speaker, hearer, x))])  
       ? $\langle do_{S\&H}(\text{make-go}) \rangle$ ( $\langle f_2 \rangle$ ); put?ABS&H([s1:(named(x, "Eleni"))])  
       ? $\langle do_{S\&H}(\text{make-go}) \rangle$ ; put?([s3:(scared(Pipkin, x))])  
       ? $\langle do_{Pipkin}(\text{run}) \rangle$ ⊤  $\wedge$  [ $do_{Pipkin}(\text{avoid-Eleni})$ ]⊥  
       ...  
ELSE   abort
```


conclusion

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Thank you for your attention!

- 1 DS-TTR
- 2 Zoom into trees and treenodes
- 3 DS-TTR+
- 4 Appendix**

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